

## 流体エンジン CIP 法 + MOC-CT

ver. 0.2

## 1 はじめに

このモジュールは、流体力学方程式・MHD 方程式を CIP + MOCCT 法で解くためのものです。

## 2 基礎方程式

以下で  $\gamma =$  定数 は比熱比、他の記号は通常の意味。

## 2.1 サブルーチン cip\_a ; 移流

$$\frac{\partial}{\partial t}(\rho) + V_x \frac{\partial}{\partial x}(\rho) = -\rho \frac{\partial}{\partial x}(V_x) \quad (1)$$

## 2.2 サブルーチン cip\_h ; 流体

$$\frac{\partial}{\partial t}(\rho) + V_x \frac{\partial}{\partial x}(\rho) = -\rho \frac{\partial}{\partial x}(V_x) \quad (2)$$

$$\frac{\partial}{\partial t}(V_x) + V_x \frac{\partial}{\partial x}(V_x) = -\frac{1}{\rho} \frac{\partial}{\partial x}(p) \quad (3)$$

$$\frac{\partial}{\partial t}(T) + V_x \frac{\partial}{\partial x}(T) = -(\gamma - 1)T \frac{\partial}{\partial x}(V_x) \quad (4)$$

$$p = \frac{k_B}{m} \rho T \quad (5)$$

## 2.3 サブルーチン cip\_h\_g ; 流体重力

$$\frac{\partial}{\partial t}(\rho) + V_x \frac{\partial}{\partial x}(\rho) = -\rho \frac{\partial}{\partial x}(V_x) \quad (6)$$

$$\frac{\partial}{\partial t}(V_x) + V_x \frac{\partial}{\partial x}(V_x) = -\frac{1}{\rho} \frac{\partial}{\partial x}(p) + g \quad (7)$$

$$\frac{\partial}{\partial t}(T) + V_x \frac{\partial}{\partial x}(T) = -(\gamma - 1)T \frac{\partial}{\partial x}(V_x) \quad (8)$$

$$p = \frac{k_B}{m} \rho T \quad (9)$$

## 2.4 サブルーチン cip\_h\_c ; 流体非一様断面

$$\frac{\partial}{\partial t}(\rho) + V_x \frac{\partial}{\partial x}(\rho) = -\frac{\rho}{S} \frac{\partial}{\partial x}(V_x S) \quad (10)$$

$$\frac{\partial}{\partial t}(V_x) + V_x \frac{\partial}{\partial x}(V_x) = -\frac{1}{\rho} \frac{\partial}{\partial x}(p) \quad (11)$$

$$\frac{\partial}{\partial t}(T) + V_x \frac{\partial}{\partial x}(T) = -(\gamma - 1) \frac{T}{S} \frac{\partial}{\partial x}(V_x S) \quad (12)$$

$$p = \frac{k_B}{m} \rho T \quad (13)$$

$S$  は断面積、

## 2.5 サブルーチン cip\_h\_cg ; 流体非一様断面重力

$$\frac{\partial}{\partial t}(\rho) + V_x \frac{\partial}{\partial x}(\rho) = -\frac{\rho}{S} \frac{\partial}{\partial x}(V_x S) \quad (14)$$

$$\frac{\partial}{\partial t}(V_x) + V_x \frac{\partial}{\partial x}(V_x) = -\frac{1}{\rho} \frac{\partial}{\partial x}(p) + g \quad (15)$$

$$\frac{\partial}{\partial t}(T) + V_x \frac{\partial}{\partial x}(T) = -(\gamma - 1) \frac{T}{S} \frac{\partial}{\partial x}(V_x S) \quad (16)$$

$$p = \frac{k_B}{m} \rho T \quad (17)$$

$S$  は断面積、

## 2.6 サブルーチン cip\_ht ; 等温流体

$$\frac{\partial}{\partial t}(\rho) + V_x \frac{\partial}{\partial x}(\rho) = -\rho \frac{\partial}{\partial x}(V_x) \quad (18)$$

$$\frac{\partial}{\partial t}(V_x) + V_x \frac{\partial}{\partial x}(V_x) = -\frac{1}{\rho} \frac{\partial}{\partial x}(p) \quad (19)$$

$$p = \frac{k_B}{m} \rho T \quad (20)$$

## 2.7 サブルーチン cip\_ht\_g ; 等温流体重力

$$\frac{\partial}{\partial t}(\rho) + V_x \frac{\partial}{\partial x}(\rho) = -\rho \frac{\partial}{\partial x}(V_x) \quad (21)$$

$$\frac{\partial}{\partial t}(V_x) + V_x \frac{\partial}{\partial x}(V_x) = -\frac{1}{\rho} \frac{\partial}{\partial x}(p) + g \quad (22)$$

$$p = \frac{k_B}{m} \rho T \quad (23)$$

## 2.8 サブルーチン cip\_ht\_c ; 等温流体非一様断面

$$\frac{\partial}{\partial t}(\rho) + V_x \frac{\partial}{\partial x}(\rho) = -\frac{\rho}{S} \frac{\partial}{\partial x}(V_x S) \quad (24)$$

$$\frac{\partial}{\partial t}(V_x) + V_x \frac{\partial}{\partial x}(V_x) = -\frac{1}{\rho} \frac{\partial}{\partial x}(p) \quad (25)$$

$$p = \frac{k_B}{m} \rho T \quad (26)$$

$S$  は断面積、

## 2.9 サブルーチン cip\_ht\_cg ; 等温流体非一様断面重力

$$\frac{\partial}{\partial t}(\rho) + V_x \frac{\partial}{\partial x}(\rho) = -\frac{\rho}{S} \frac{\partial}{\partial x}(V_x S) \quad (27)$$

$$\frac{\partial}{\partial t}(V_x) + V_x \frac{\partial}{\partial x}(V_x) = -\frac{1}{\rho} \frac{\partial}{\partial x}(p) + g \quad (28)$$

$$p = \frac{k_B}{m} \rho T \quad (29)$$

$S$  は断面積、温度  $T$  は既知の定数。

## 2.10 サブルーチン cip\_m ; MHD

$$\frac{\partial \rho}{\partial t} + V_x \frac{\partial \rho}{\partial x} = -\rho \frac{\partial V_x}{\partial x} \quad (30)$$

$$\frac{\partial V_x}{\partial t} + V_x \frac{\partial V_x}{\partial x} = -\frac{1}{\rho} \frac{\partial p}{\partial x} - \frac{1}{4\pi\rho} B_y \frac{\partial B_y}{\partial x} \quad (31)$$

$$\frac{\partial V_y}{\partial t} + V_x \frac{\partial V_y}{\partial x} = \frac{1}{4\pi\rho} B_x \frac{\partial B_y}{\partial x} \quad (32)$$

$$\frac{\partial T}{\partial t} + V_x \frac{\partial T}{\partial x} = -(\gamma - 1)T \frac{\partial V_x}{\partial x} \quad (33)$$

$$\frac{\partial B_y}{\partial t} = \frac{\partial E_z}{\partial x} \quad (34)$$

$$E_z = -V_x B_y + V_y B_x \quad (35)$$

$$p = \frac{k_B}{m} \rho T \quad (36)$$

磁場  $B_x$  は既知の定数。

## 2.11 サブルーチン cip\_m\_g ; MHD 重力

$$\frac{\partial \rho}{\partial t} + V_x \frac{\partial \rho}{\partial x} = -\rho \frac{\partial V_x}{\partial x} \quad (37)$$

$$\frac{\partial V_x}{\partial t} + V_x \frac{\partial V_x}{\partial x} = -\frac{1}{\rho} \frac{\partial p}{\partial x} - \frac{1}{4\pi\rho} B_y \frac{\partial B_y}{\partial x} + g_x \quad (38)$$

$$\frac{\partial V_y}{\partial t} + V_x \frac{\partial V_y}{\partial x} = \frac{1}{4\pi\rho} B_x \frac{\partial B_y}{\partial x} + g_y \quad (39)$$

$$\frac{\partial T}{\partial t} + V_x \frac{\partial T}{\partial x} = -(\gamma - 1)T \frac{\partial V_x}{\partial x} \quad (40)$$

$$\frac{\partial B_y}{\partial t} = \frac{\partial E_z}{\partial x} \quad (41)$$

$$E_z = -V_x B_y + V_y B_x \quad (42)$$

$$p = \frac{k_B}{m} \rho T \quad (43)$$

磁場  $B_x$  は既知の定数。

## 2.12 サブルーチン cip\_m\_c ; MHD 非一様断面

$$\frac{\partial \rho}{\partial t} + V_x \frac{\partial \rho}{\partial x} = -\frac{\rho}{S} \frac{\partial (V_x S)}{\partial x} \quad (44)$$

$$\frac{\partial V_x}{\partial t} + V_x \frac{\partial V_x}{\partial x} = -\frac{1}{\rho} \frac{\partial p}{\partial x} - \frac{1}{4\pi\rho} B_y \frac{\partial B_y}{\partial x} \quad (45)$$

$$\frac{\partial V_y}{\partial t} + V_x \frac{\partial V_y}{\partial x} = \frac{1}{4\pi\rho} B_x \frac{\partial B_y}{\partial x} \quad (46)$$

$$\frac{\partial T}{\partial t} + V_x \frac{\partial T}{\partial x} = -(\gamma - 1) \frac{T}{S} \frac{\partial (V_x S)}{\partial x} \quad (47)$$

$$\frac{\partial (B_y S)}{\partial t} = \frac{\partial (E_z S)}{\partial x} \quad (48)$$

$$E_z = -V_x B_y + V_y B_x \quad (49)$$

$$p = \frac{k_B}{m} \rho T \quad (50)$$

$B_x$  は既知で  $S \propto 1/B_x$  は断面積。

### 2.13 サブルーチン cip\_m\_cg ; MHD 非一様断面重力

$$\frac{\partial \rho}{\partial t} + V_x \frac{\partial \rho}{\partial x} = -\frac{\rho}{S} \frac{\partial (V_x S)}{\partial x} \quad (51)$$

$$\frac{\partial V_x}{\partial t} + V_x \frac{\partial V_x}{\partial x} = -\frac{1}{\rho} \frac{\partial p}{\partial x} - \frac{1}{4\pi\rho} B_y \frac{\partial B_y}{\partial x} + g_x \quad (52)$$

$$\frac{\partial V_y}{\partial t} + V_x \frac{\partial V_y}{\partial x} = \frac{1}{4\pi\rho} B_x \frac{\partial B_y}{\partial x} + g_y \quad (53)$$

$$\frac{\partial T}{\partial t} + V_x \frac{\partial T}{\partial x} = -(\gamma - 1) \frac{T}{S} \frac{\partial (V_x S)}{\partial x} \quad (54)$$

$$\frac{\partial (B_y S)}{\partial t} = \frac{\partial (E_z S)}{\partial x} \quad (55)$$

$$E_z = -V_x B_y + V_y B_x \quad (56)$$

$$p = \frac{k_B}{m} \rho T \quad (57)$$

$B_x$  は既知で  $S \propto 1/B_x$  は断面積。

### 2.14 サブルーチン cip\_m\_cgr ; MHD 非一様断面重力回転

$$\frac{\partial \rho}{\partial t} + V_x \frac{\partial \rho}{\partial x} = -\frac{\rho}{S} \frac{\partial (V_x S)}{\partial x} \quad (58)$$

$$\frac{\partial V_x}{\partial t} + V_x \frac{\partial V_x}{\partial x} = -\frac{1}{\rho} \frac{\partial p}{\partial x} - \frac{1}{4\pi\rho} \frac{B_y}{R} \frac{\partial (B_y R)}{\partial x} + \frac{V_y^2}{R} \frac{\partial R}{\partial x} + g_x \quad (59)$$

$$\frac{\partial (V_y R)}{\partial t} + V_x \frac{\partial (V_y R)}{\partial x} = \frac{1}{4\pi\rho} B_x \frac{\partial (B_y R)}{\partial x} \quad (60)$$

$$\frac{\partial T}{\partial t} + V_x \frac{\partial T}{\partial x} = -(\gamma - 1) \frac{T}{S} \frac{\partial (V_x S)}{\partial x} \quad (61)$$

$$\frac{\partial}{\partial t} \left( \frac{B_y S}{R} \right) = \frac{\partial}{\partial x} \left( \frac{E_z S}{R} \right) \quad (62)$$

$$E_z = -V_x B_y + V_y B_x \quad (63)$$

$$p = \frac{k_B}{m} \rho T \quad (64)$$

$B_x$  は既知で  $S \propto 1/B_x$  は断面積。

## 2.15 サブルーチン cip\_m3 ; 3 成分 MHD

$$\frac{\partial \rho}{\partial t} + V_x \frac{\partial \rho}{\partial x} = -\rho \frac{\partial V_x}{\partial x} \quad (65)$$

$$\frac{\partial V_x}{\partial t} + V_x \frac{\partial V_x}{\partial x} = -\frac{1}{\rho} \frac{\partial p}{\partial x} - \frac{1}{4\pi\rho} \left( B_y \frac{\partial B_y}{\partial x} + B_z \frac{\partial B_z}{\partial x} \right) \quad (66)$$

$$\frac{\partial V_y}{\partial t} + V_x \frac{\partial V_y}{\partial x} = \frac{1}{4\pi\rho} B_x \frac{\partial B_y}{\partial x} \quad (67)$$

$$\frac{\partial V_z}{\partial t} + V_x \frac{\partial V_z}{\partial x} = \frac{1}{4\pi\rho} B_x \frac{\partial B_z}{\partial x} \quad (68)$$

$$\frac{\partial T}{\partial t} + V_x \frac{\partial T}{\partial x} = -(\gamma - 1)T \frac{\partial V_x}{\partial x} \quad (69)$$

$$\frac{\partial B_y}{\partial t} = \frac{\partial E_z}{\partial x} \quad (70)$$

$$\frac{\partial B_z}{\partial t} = -\frac{\partial E_y}{\partial x} \quad (71)$$

$$E_y = -V_z B_x + V_x B_z, \quad E_z = -V_x B_y + V_y B_x \quad (72)$$

$$p = \frac{k_B}{m} \rho T \quad (73)$$

磁場  $B_x$  は既知の定数。

## 2.16 サブルーチン cip\_m3\_g ; 3 成分 MHD 重力

$$\frac{\partial \rho}{\partial t} + V_x \frac{\partial \rho}{\partial x} = -\rho \frac{\partial V_x}{\partial x} \quad (74)$$

$$\frac{\partial V_x}{\partial t} + V_x \frac{\partial V_x}{\partial x} = -\frac{1}{\rho} \frac{\partial p}{\partial x} - \frac{1}{4\pi\rho} \left( B_y \frac{\partial B_y}{\partial x} + B_z \frac{\partial B_z}{\partial x} \right) + g_x \quad (75)$$

$$\frac{\partial V_y}{\partial t} + V_x \frac{\partial V_y}{\partial x} = \frac{1}{4\pi\rho} B_x \frac{\partial B_y}{\partial x} + g_y \quad (76)$$

$$\frac{\partial V_z}{\partial t} + V_x \frac{\partial V_z}{\partial x} = \frac{1}{4\pi\rho} B_x \frac{\partial B_z}{\partial x} + g_z \quad (77)$$

$$\frac{\partial T}{\partial t} + V_x \frac{\partial T}{\partial x} = -(\gamma - 1)T \frac{\partial V_x}{\partial x} \quad (78)$$

$$\frac{\partial B_y}{\partial t} = \frac{\partial E_z}{\partial x} \quad (79)$$

$$\frac{\partial B_z}{\partial t} = -\frac{\partial E_y}{\partial x} \quad (80)$$

$$E_y = -V_z B_x + V_x B_z, \quad E_z = -V_x B_y + V_y B_x \quad (81)$$

$$p = \frac{k_B}{m} \rho T \quad (82)$$

磁場  $B_x$  は既知の定数。

## 2.17 サブルーチン cip\_m3\_c ; 3 成分 MHD 非一様断面

$$\frac{\partial \rho}{\partial t} + V_x \frac{\partial \rho}{\partial x} = -\frac{\rho}{S} \frac{\partial(V_x S)}{\partial x} \quad (83)$$

$$\frac{\partial V_x}{\partial t} + V_x \frac{\partial V_x}{\partial x} = -\frac{1}{\rho} \frac{\partial p}{\partial x} - \frac{1}{4\pi\rho} \left( B_y \frac{\partial B_y}{\partial x} + B_z \frac{\partial B_z}{\partial x} \right) \quad (84)$$

$$\frac{\partial V_y}{\partial t} + V_x \frac{\partial V_y}{\partial x} = \frac{1}{4\pi\rho} B_x \frac{\partial B_y}{\partial x} \quad (85)$$

$$\frac{\partial V_z}{\partial t} + V_x \frac{\partial V_z}{\partial x} = \frac{1}{4\pi\rho} B_x \frac{\partial B_z}{\partial x} \quad (86)$$

$$\frac{\partial T}{\partial t} + V_x \frac{\partial T}{\partial x} = -(\gamma - 1) \frac{T}{S} \frac{\partial(V_x S)}{\partial x} \quad (87)$$

$$\frac{\partial(B_y S)}{\partial t} = \frac{\partial(E_z S)}{\partial x} \quad (88)$$

$$\frac{\partial(B_z S)}{\partial t} = -\frac{\partial(E_y S)}{\partial x} \quad (89)$$

$$E_y = -V_z B_x + V_x B_z, \quad E_z = -V_x B_y + V_y B_x \quad (90)$$

$$p = \frac{k_B}{m} \rho T \quad (91)$$

磁場  $B_x$  は既知の定数。

## 2.18 サブルーチン cip\_m\_cg ; 3 成分 MHD 非一様断面重力

$$\frac{\partial \rho}{\partial t} + V_x \frac{\partial \rho}{\partial x} = -\frac{\rho}{S} \frac{\partial(V_x S)}{\partial x} \quad (92)$$

$$\frac{\partial V_x}{\partial t} + V_x \frac{\partial V_x}{\partial x} = -\frac{1}{\rho} \frac{\partial p}{\partial x} - \frac{1}{4\pi\rho} \left( B_y \frac{\partial B_y}{\partial x} + B_z \frac{\partial B_z}{\partial x} \right) + g_x \quad (93)$$

$$\frac{\partial V_y}{\partial t} + V_x \frac{\partial V_y}{\partial x} = \frac{1}{4\pi\rho} B_x \frac{\partial B_y}{\partial x} + g_y \quad (94)$$

$$\frac{\partial V_z}{\partial t} + V_x \frac{\partial V_z}{\partial x} = \frac{1}{4\pi\rho} B_x \frac{\partial B_z}{\partial x} + g_z \quad (95)$$

$$\frac{\partial T}{\partial t} + V_x \frac{\partial T}{\partial x} = -(\gamma - 1) \frac{T}{S} \frac{\partial(V_x S)}{\partial x} \quad (96)$$

$$\frac{\partial(B_y S)}{\partial t} = \frac{\partial(E_z S)}{\partial x} \quad (97)$$

$$\frac{\partial(B_z S)}{\partial t} = -\frac{\partial(E_y S)}{\partial x} \quad (98)$$

$$E_y = -V_z B_x + V_x B_z, \quad E_z = -V_x B_y + V_y B_x \quad (99)$$

$$p = \frac{k_B}{m} \rho T \quad (100)$$

磁場  $B_x$  は既知の定数。